

QB365
Important Questions - Number Systems

9th Standard CBSE

Mathematics

Reg.No. :

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Time : 01:00:00 Hrs

Total Marks : 50

Section-A

- 1) Which of the following is a rational number? 1
 (a) $1 + \sqrt{3}$ (b) π (c) $2\sqrt{3}$ (d) 0
- 2) A rational number lying between $\sqrt{2}$ and $\sqrt{3}$ is: 1
 (a) $\frac{\sqrt{2}+\sqrt{3}}{2}$ (b) $\sqrt{6}$ (c) 1.6 (d) 1.9
- 3) Two rational numbers between $\frac{2}{3}$ and $\frac{5}{3}$ are: 1
 (a) $\frac{1}{6}$ and $\frac{2}{6}$ (b) $\frac{1}{2}$ and $\frac{2}{7}$ (c) $\frac{5}{6}$ and $\frac{7}{6}$ (d) $\frac{2}{3}$ and $\frac{4}{3}$
- 4) Which of the following is a rational number? 1
 (a) $\sqrt{5}$ (b) π (c) 0.101 001 0001 00001... (d) 0.853 853 853....
- 5) Which one of the following is an irrational number? 1
 (a) 0.14 (b) $0.\overline{1416}$ (c) $0.\overline{1416}$ (d) 0.401 4001 40001 4...
- 6) $(\sqrt{a} + \sqrt{b})(\sqrt{a} - \sqrt{b})$ is: 1
 (a) $a+b$ (b) $a-b$ (c) $2\sqrt{a}$ (d) $2\sqrt{b}$
- 7) Which of the following numbers is an irrational number? 1
 (a) $\sqrt{16} - 4$ (b) $(3 - \sqrt{3})(3 + \sqrt{3})$ (c) $\sqrt{5} + 3$ (d) $-\sqrt{25}$
- 8) The value of $\frac{2^0+7^0}{5^0}$ is: 1
 (a) 2 (b) 0 (c) $9/5$ (d) $1/5$
- 9) The value of $\sqrt[4]{(64)^{-2}}$ is 1
 (a) $1/8$ (b) $1/2$ (c) 8 (d) $1/64$
- 10) Value of $\left[\left(81^{-1/2} \right)^{\frac{-1}{4}} \right]^2$ is: 1
 (a) 3 (b) $1/3$ (c) 9 (d) $1/9$

Section-B

- 11) Find two rational numbers between 0.1 and 0.2. 2
- 12) Check whether $7\sqrt{5}$, $\frac{7}{\sqrt{5}} \cdot \sqrt{2} + 21$, $\pi - 5$ are irrational numbers or not. 2
- 13) Divide $8\sqrt{15}$ by $2\sqrt{3}$ 2
- 14) Simplify:
 (i) $17^2 \cdot 17^5$
- 15) Simplify: $\frac{23^{-10}}{23^7}$ 2

- 16) Rationalize the denominator of $\frac{1}{\sqrt{2}}$ 2
- 17) If $a = 5 + 2\sqrt{6}$ and $b = \frac{1}{a}$ then what will be the value of $a^2 + b^2$ and $a^3 + b^3$? 2
- 18) Simplify: $\left(\frac{\frac{1}{15} \cdot 3}{\frac{1}{9} \cdot 4} \right)^{-6}$ 2
- 19) If $(4)^{2x-1} - (16)^{x-1} = 384$, then find the value of x. 2
- 20) Evaluate: $\frac{\sqrt{5}+\sqrt{3}}{\sqrt{5}-\sqrt{3}}$, given that $\sqrt{15} = 3.87$ 2

Section-C

- 21) Find four rational numbers between $\frac{1}{3}$ and $\frac{4}{5}$ 5
- 22) $\frac{\sqrt{147}}{\sqrt{75}}$ is not a rational number as $\sqrt{147}$ and $\sqrt{75}$ are not rational. State whether it is true or false. Justify your answer. 5
- 23) Find the values of a and b if: $\frac{7+3\sqrt{5}}{3+\sqrt{5}} - \frac{7-3\sqrt{5}}{3-\sqrt{5}} = a + \sqrt{5}b$ 5
- 24) Simplify: $\left(\frac{81}{16} \right)^{-\frac{3}{4}} \times \left(\frac{25}{9} \right)^{-\frac{3}{2}}$ 5

Section-A

- 1) (d) 0 1
- 2) (c) 1.6 1
- 3) (c) $5/6$ and $7/6$ 1
- 4) (d) 0.853 853 853.... 1
- 5) (d) 0.401 4001 40001 4... 1
- 6) (c) $2\sqrt{a}$ 1
- 7) (a) $\sqrt{16} - 4$ 1
- 8) (a) 2 1
- 9) (a) $1/8$ 1
- 10) (a) 3 1

Section-B

- 11) 0.125, 0.15 2
- 12) All are irrational numbers. 2
- 13) $4\sqrt{5}$ 2
- 14) 17^7 2
- 15) 23^{-17} 2
- 16) $\frac{\sqrt{2}}{2}$ 2
- 17) 98, 970 2
- 18) $\frac{27}{225}$ 2
- 19) $\frac{11}{4}$ 2

Section-C

21) $\frac{1}{3} = \frac{1 \times 5}{3 \times 5} = \frac{5}{15}$

5

$\frac{4}{5} = \frac{4 \times 3}{5 \times 3} = \frac{12}{15}$

$5 < 6 < 7 < 8 < 9 < 12$

$\frac{5}{15} < \frac{6}{12} < \frac{7}{12} < \frac{8}{12} < \frac{9}{12} < \frac{12}{15}$

$\frac{1}{3} < \frac{1}{2} < \frac{7}{12} < \frac{2}{3} < \frac{3}{4} < \frac{4}{5}$

Hence, four rational numbers between $\frac{1}{3}$ and $\frac{4}{5}$ can be taken as $\frac{1}{2}$, $\frac{7}{12}$, $\frac{2}{3}$ and $\frac{3}{4}$

22)

5

$$\frac{\sqrt{147}}{\sqrt{75}} = \frac{\sqrt{3 \times 7 \times 7}}{\sqrt{3 \times 5 \times 5}} = \frac{7\sqrt{3}}{5\sqrt{3}} = \frac{7}{5}$$

which is clearly a rational number.

Hence, the given statement is false. The reason is that 'if we divide two irrationals, the result may be rational or irrational'!

23) $\frac{7+3\sqrt{5}}{3+\sqrt{5}} - \frac{7-3\sqrt{5}}{3-\sqrt{5}} = a + \sqrt{5}b$

5

$$\frac{(7+3\sqrt{5})(3-\sqrt{5})}{(3+\sqrt{5})(3-\sqrt{5})} - \frac{(7+3\sqrt{5})(3+\sqrt{5})}{(3+\sqrt{5})(3+\sqrt{5})}$$

$$= \frac{21-7\sqrt{5}+9\sqrt{5}-15}{9-5} - \frac{21+7\sqrt{5}+9\sqrt{5}-15}{9-5}$$

$$= a + 5\sqrt{b}$$

$$\frac{6+2\sqrt{5}}{4} - \frac{6-2\sqrt{5}}{4} = a + \sqrt{5}b$$

$$= \frac{(6+2\sqrt{5})-(6-2\sqrt{5})}{4} = a + \sqrt{5}b$$

$$\frac{4\sqrt{5}}{4} = a + \sqrt{5}b$$

$$\sqrt{5} = a + \sqrt{5}b$$

$$a = 0, b = 1$$

24)
$$\left(\frac{81}{16}\right)^{-\frac{3}{4}} \times \left(\frac{25}{9}\right)^{-\frac{3}{2}}$$

5

$$= \left\{ \left(\frac{81}{16}\right)^4 \right\}^{-\frac{3}{4}} \times \left\{ \left(\frac{5}{3}\right)^2 \right\}^{-\frac{3}{2}}$$

$$= \left(\frac{3}{2}\right)^{4 \times (-\frac{3}{4})} \times \left(\frac{5}{2}\right)^{2 \times (-\frac{3}{2})}$$

$$= \left(\frac{3}{2}\right)^{-3} \times \left(\frac{5}{3}\right)^{-3} = \left(\frac{3}{2} \times \frac{5}{3}\right)^{-3}$$

$$= \left(\frac{5}{3}\right)^{-3} = \left(\frac{2}{5}\right)^{-3} = \frac{8}{125}$$

