## QB365

# Model Question Paper 2

### 9th Standard CBSE

Mathematics Reg.No.:
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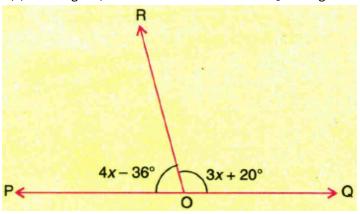
Time: 02:00:00 Hrs

Total Marks: 100

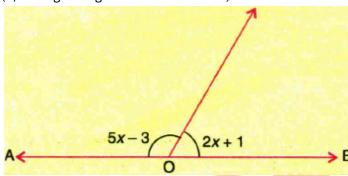
## **Section-A**

1) An obtuse angle	1
(a) measures between $0^0$ and $90^0$ (b) is greater than $90^0$ but less than $180^0$ (c) is exactly equal to $90^0$	
(d) is exactly equal to $180^{0}$	
2) Two angles whose sum is $90^0$ are called	1
(a) supplementary angles (b) complement <mark>ary angles (c)</mark> corres <mark>pondi</mark> ng angles (d) alternate angles	
3) The angles whose sum is $180^0$ are called	1
(a) supplementary angles (b) complementary angles (c) alternate angles (d) corresponding angles	
4) A reflex angle	1
(a) is greater than $180^0$ but less than $360^0$ (b) is exactly equal to $180^0$ (c) is exactly equal to $90^0$	
(d) is greater than $90^0$ but less than $180^0$ 5) Two angles whose sum is $90^0$ are called	
5) Two angles whose sum is $90^0$ are called	1
(a) Supplementary angles (b) complimentary angles (c) corresponding angles (d) alternate angles	
6) An angle which is exactly equal to $90^0$ is called	1
(a) an obtuse angle (b) an acute angle (c) a straight angle (d) a right angle	
7) The angle supplementary to $60^0$ is	1
(a) $30^0$ (b) $120^0$ (c) $45^0$ (d) $300^0$	
8) The compliment of $(90^0-a^0)$ is	1
(a) $-a^0$ (b) $90^0 + a^0$ (c) $90^0 - a^0$ (d) $a^0$	
9) The angle of supplementary to $90^0+9^0$ is	1
(a) $90^0 + 9^0$ (b) $90^0 - 9^0$ (c) $180^0 - +9^0$ (d) $180^0 - 9^0$	
10) Which of the following is not a pair of complementary angles?	1
(a) $60^0$ , $30^0$ (b) $56^0$ , $34^0$ (c) $0^0$ , $90^0$ (d) $150^0$ , $30^0$	
11) if the measure of an angle is twice the measure of its supplementary angle, then the measure of the angle is	1
(a) $60^0$ (b) $90^0$ (c) $120^0$ (d) $80^0$	
12) The angle which exceeds its complimentary angle by $30^{0}$	1
(a) $50^0$ (b) $120^0$ (c) $60^0$ (d) $80^0$	

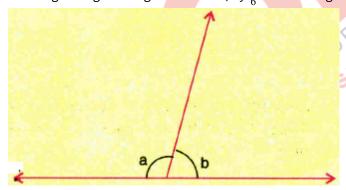
13) Two complementary angles are in the ratio 4:5 then angles are:	1
(a) $90^0$ , $90^0$ (b) $40^0$ , $50^0$ (c) $30^0$ , $150^0$ (d) $45^0$ , $45^0$	
14) We can draw two different lines in	1
(a) Only one way (b) two different ways (c) three different ways (d) None of these	
15) A line indicates	1
(a) Only one direction (b) two directions (c) no direction (d) None of these	
16) In the following figure $\angle AOB$ and $\angle BOC$ are:	1
C	
A O B	
(a) Supplementary angles (b) complementary angles (c) adjacent angles (d) None of these	
17) A pair of angles is called linear pair if the sum of two adjacent angles is:	1
(a) $90^0$ (b) $180^0$ (c) $230^0$ (d) $360^0$	
(a) 90° (b) 180° (c) 230° (d) 360°  18) The value of x in figure is:  (a) 80° (b) 20° (c) 25° (d) 40°  19) In figure the value x is  (a) 30° (b) 10° (c) 20° (d) 40°  20) If two parallel lines are intersected by a transversal then corresponding angles are:	1
(a) $80^0$ (b) $20^0$ (c) $25^0$ (d) $40^0$	
19) In figure the value x is	1
(a) $30^0$ (b) $10^0$ (c) $20^0$ (d) $40^0$	
20) If two parallel lines are intersected by a transversal then corresponding angles are:	1
(a) Equal (b) Complimentary (c) Supplementary (d) Sum of the two angles is 360°	
Section-B	
21) Two complementary angles are such that two times the measure of one to three times the measure of the	2
other .Find the measure of the largest angle.	
22) If $(3x-58^0)$ and $(x+38^0)$ are supplementary angles, find x and the angles.	2



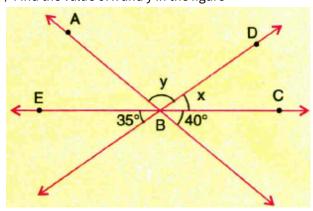
(b)In the given figure find the value of x,If AOB is a line



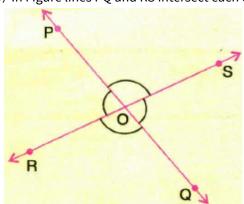
<sup>24)</sup> In the given figure a is greater than b, by  $\frac{1}{6}$  th of a straight angle Find the angles of a and b.



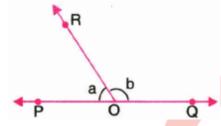
25) Find the value of x and y in the figure



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- 27) An exterior angle of a triangle is  $115^0$  and one of the interior opposite angles is  $35^0$  Find the other two angles of the triangle
- 28) In figure  $\angle B = 55^{\circ}$ ,  $\angle C = 45^{\circ}$  and the bisector of  $\angle$  A meets BC at D ,find  $\angle$  ADB and  $\angle$  ADC
- 29) An angle is equal to five times its supplement. Find the measure of the angle
- 30) In figure  $\angle POR$  and  $\angle QOR$  form a linear pair. If b-a= $60^{\circ}$  find the values of a and b.



31) In  $\triangle$  ABC if  $\angle A = (2Xx - 5)^0$ ,  $\angle B = (5X + 5)^0 \angle C = (3Xx - 50)^0$  then find the values of x, $\angle$  A, $\angle$ B and  $\angle$ C

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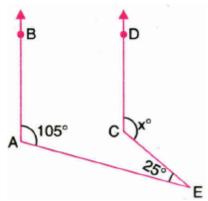
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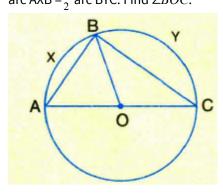
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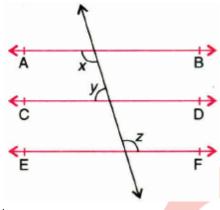
- 32) find the angles of a traingle PQR if  $\angle p \angle q = 45^{\circ}$  and  $\angle Q \angle R = 30^{\circ}$
- 33) Let OA,AB,OC and OD be the rays in the anticlockwise direction starting from OA, such that  $\angle AOB = \angle COD = 100^0$ ;  $\angle AOD = \angle BOC = 80^0$  Is it true that AOC and BOD are straight lines? Justify your answer by drawing by drawing the figures.
- 34) In the given figure AB  $\parallel$  C Find the value of x.



- 35) In  $\triangle PQR$ ,  $\angle P = 100^{\circ}$  and  $\angle R = 60^{\circ}$ , which side of the triangle is the longest. Give reasons for your answer.
- 36) In a parallelogram PQRS, if ∠QRS=2x, ∠PQS=4x, and ∠PSQ=4x, find the angles of the parallelogram.
- 37) If an angle of a parallelogram in two-third of its adjacent angle then find the measure of all the angles,

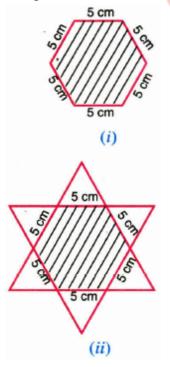


39) In figure if  $AB \parallel CD \parallel$  ,  $CD \parallel EF$  and y:z=3:7, find x



40) Complete the hexagonal and star shaped Rangolies [see figures (i) and (ii)] by filling them with as many equilateral triangles of side 1em as you can. Count the number of triangles in each case. Which has more

triangles?



**Section-C** 

41) ABCD is a cyclic trapezium with AD  $\parallel$  BC. If  $\angle B$  = 70°, determine other three angles of the trapezium.

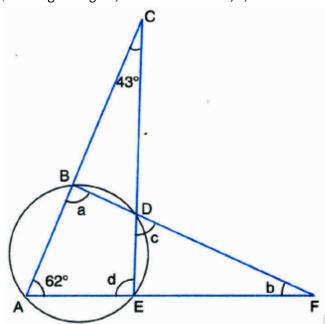
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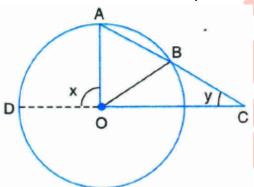
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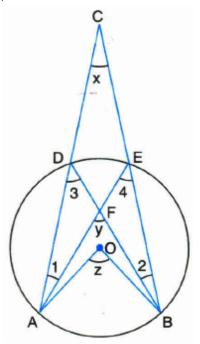
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43) In the figure, chord AB of a circle with centre O, is produced to C such that BC = OB. CO is joined and produced to meet the circle in D. If  $\angle ACD = y$  and  $\angle AOD = x$ , show that x = 3y.



- 44) Prove that the opposite angles of an isosceles trapezium are supplementary.
- 45) ABCD is a cyclic quadrilateral. If AC bisects both the angles A and C then prove that  $\angle ABC = 90^{\circ}$ .
- 46) ABC is a triangle and P is a point on the side BC such that AB = AP. If AP produced meets the circumcircle of  $\triangle ABC$  at Q, prove that CP = CQ.
- 47) D is a point on the circumference of circumcircle of  $\triangle ABC$  in which AB =AC such that Band D are on opposite sides of AC. If CD is produced to point E such that CE = BD, prove that AD = AE.



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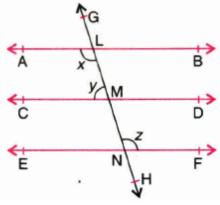
#### Section-A

Section-A
1) (b) is greater than $90^0$ but less than $180^0$
1) (b) is greater than 90° but less than 180° 2) (b) complementary angles 3) (a) supplementary angles 4) (a) is greater than 180° but less than 360° 5) (b) complimentary angles
3) (a) supplementary angles
4) (a) is greater than $180^0$ but less than $360^0$
5) (b) complimentary angles
6) (d) a right angle
7) (b) 120 <sup>0</sup>
8) (d) $a^0$
9) (a) $90^0 + 9^0$
10) (a) $60^0$ , $30^0$
11) (c) $120^0$
12) (c) $60^0$
13) (b) $40^0$ , $50^0$
14) (b) two different ways
15) (b) two directions
16) (d) None of these
17) (b) $180^{0}$
18) (b) 20 <sup>0</sup>

19) (c) $20^0$	1
20) (a) Equal	1
Section-B	
21) 54 <sup>0</sup>	2
22) $x=50,92^0$ and $88^0$	2
23) (a) 28 (b) 26	2
24) Given,	2
$a-b=\frac{1}{6}\times 180^o$	
a-b=30°(1)	
a+b=180° (Linear pair)(2)	
Adding (1) & (2), 2a=210°	
a=105°	
b=180°-a=180°-105°	
=75°	
25) $X=35^{\circ} y=105^{\circ}$ 26) $\angle PQR=75^{\circ}, \angle ROQ=105^{\circ} \angle POS=105^{\circ} \angle SOQ=75^{\circ}$ 27) $80^{\circ}, 65^{\circ}$ 28) $85^{\circ}, 95^{\circ}$ 29) $150^{\circ}$ 30) $60^{\circ}, 120^{\circ}$ 31) $13; 21^{\circ}, 70^{\circ}, 89^{\circ}$ 32) $100^{\circ}, 55^{\circ}, 25^{\circ}$	2
26) $\angle PQR = 75^{\circ}, \angle ROQ = 105^{\circ} \angle POS = 105^{\circ} \angle SOQ = 75^{\circ}$	2
27) 80 <sup>0</sup> ,65 <sup>0</sup>	2
28) 85 <sup>0</sup> , 95 <sup>0</sup>	2
29) 1500	2
30) $60^0$ , $120^0$	2
31) 13; 21 <sup>0</sup> , 70 <sup>0</sup> , 89 <sup>0</sup>	2
32) 100 <sup>0</sup> , 55 <sup>0</sup> , 25 <sup>0</sup>	2
33) Yes! AOC and BOD both are straight lines	2
34) <sub>130</sub> 0	2
35) QR as ∠P is the greatest	2
36) 36°,144°,36°, 144°	2

37) 72°, 108°, 72°, 108°

38) 120°



and  $: AB \parallel CD$   $CD \parallel EF : AB \parallel EF$ 

Lines parallel to the same line are parallel to each other

$$x = 2$$

Alternate Interior Angles

$$X+y=180^{0}$$

Consecutive interior angles on the same side of a transversal GH to parallel lines AB and CD

From (1) and (2)

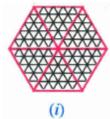
$$z+y=180^{0}$$

Sum of the ratios=3+7=10

$$\therefore y = \frac{3}{10}X180^0 = 54^0$$
and  $z = \frac{7}{10}x180^0 = 126^0 \therefore x = z = 126^0$ 

40) (i) Number of triangles =  $25 \times 6$ 

$$= 25 + 25 + 25 + 25 + 25 + 25 = 150$$



(ii) Number of triangles =  $25 \times 6 + 25 \times 6$ 



Figure (ii) has more triangles.

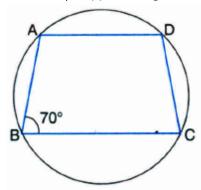
AD || BC. 
$$\angle B = 70^{\circ}$$
.

**To determine:** Other three angles of the trapezium.

#### **Determination:**

$$\angle B + \angle D = 180^{\circ}$$

: Opposite angles of a cyclic quadrilateral are supplementary



$$\Rightarrow 70^{\circ} \angle D = 180^{\circ}$$

$$\Rightarrow \angle D = 180^{\circ} - 70^{\circ}$$

$$\Rightarrow \angle D = 110^{\circ}$$

Again, ∵ AD || BC and transversal AB intersects them

$$\therefore \angle A + \angle B = 180^{\circ}$$

 $|\because$  The sum of the consecutive interior angles on the same side of a transversal is 180°

$$\Rightarrow \angle A + 70^{\circ} = 180^{\circ}$$

$$\Rightarrow$$
  $\angle A = 180^{\circ} - 70^{\circ}$ 

$$\Rightarrow$$
  $\angle A = 110^{\circ}$ 

Also, 
$$\angle A + \angle C = 180^{\circ}$$

: Opposite angles of a cyclic quadrilateral are supplementary

$$\Rightarrow 110^{\circ} + \angle C = 180^{\circ}$$

$$\Rightarrow$$
  $\angle C = 180^{\circ} - 110^{\circ}$ 

$$\Rightarrow$$
  $\angle C = 70^{\circ}$ .

An exterior angle of a cyclic quadrilateral is equal to its interior opposite angle

$$\Rightarrow \angle c = 62^{\circ}$$

In  $\triangle AEC$ ,

$$\angle ACE + \angle CAE + \angle d = 180^{\circ}$$

| Angle sum property of a triangle

$$\Rightarrow$$
 43° + 62° +  $\angle d$  = 180°

$$\Rightarrow$$

$$\angle d = 75^{\circ}$$
 ...(2)

$$\angle a + \angle d = 180^{\circ}$$

| Opposite angles of a cyclic quadrilateral are supplementary

$$\Rightarrow$$
  $\angle a + 75^\circ = 180^\circ$ 

$$\rightarrow$$

$$\angle a = 105^{\circ}$$

In  $\Delta FDE$ ,

$$\angle c + (180^{\circ} - \angle d) + \angle b = 180^{\circ}$$

| Angle sum property of a triangle

$$\Rightarrow$$
 62° + (180° - 75°) +  $\angle b$  = 180°

$$\Rightarrow$$
  $\angle b = 13^{\circ}$ 



**Given:** Chord AB of a circle with centre O, is produced to C such that BC = OB. CO is joined and produced to meet the circle in D.  $\angle ACD = y$  and  $\angle AOD = x$ .

**To Prove:** x = 3y

**Proof:** In  $\triangle BOC$ ,

$$\therefore \angle BOC = \angle BCO$$

Angles opposite to equal sides of a triangle are equal

$$\Rightarrow \angle BOC = y$$

In  $\triangle BOC$ ,

$$\angle OBA = \angle OBC + \angle BCO$$

: An exterior angle of a triangle is equal to the sum of its two interior opposite angles

In  $\triangle OAB$ ,

| Radii of the same circle

$$\therefore \angle OAB = 2y$$

Now, ∵ DOC is a straight line

$$\therefore$$
  $\angle AOD + \angle AOB + \angle BOC = 180^{\circ}$ 

$$\Rightarrow x + \{180^{\circ} - (\angle OAB + \angle OBA)\} + y = 180^{\circ}$$

| Angle sum property of a triangle

$$\Rightarrow$$
  $x + \{180^{\circ} - (2y + 2y)\} + y = 180^{\circ}$ 

$$x=3y$$

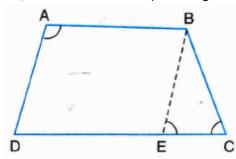
**To prove:** Opposite angles of ABCD are supplementary.

**Construction:** Draw BE || AD **Proof:** In quadrilateral ABED,

AB || DE | I Given

AD || BE | By construction

∴ Quadrilateral ABED is a parallelogram.



A quadrilateral is a parallelogram if its both the pairs of opposite sides are parallel.

$$\therefore \angle BAD = \angle BED$$

I Opposite angles of a parallelogram are equal

But AD=BC | Given

∴ BE=BC

$$\therefore \angle BEC = \angle BCE$$

| Angles opposite to equal sides of a triangle are equal

$$\therefore \quad \angle BEC = \angle BED = 180^{\circ}$$

Linear pair axiom

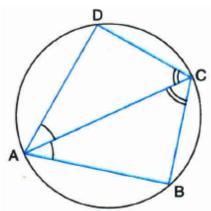
$$\Rightarrow \angle BCE + \angle BED = 180^{\circ}$$
 | From (2)

$$\Rightarrow \angle BCE + \angle BAD = 180^{\circ}$$
 | From (1)

$$\Rightarrow$$
  $\angle BCD + \angle BAD = 180^{\circ}$ 

⇒ Opposite angles of ABCD are supplementary.

**To Prove:**  $\angle ABC = 90^{\circ}$ 



Proof: In  $\triangle ADC$  and  $\triangle ABC$ ,

 $\angle DAC = \angle BAC \mid :: AC \text{ bisects angle A}$ 

 $\angle DCA = \angle BCA$ 

| ∵ AC bisects angle C

AC=AC

Common

 $\therefore \Delta ADC \cong \Delta ABC \mid ASA$  congruence rule

$$\therefore \angle ADC = \angle ABC$$

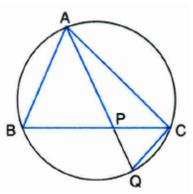
But  $\angle ADC + \angle ABC = 180^{\circ}$ 

applementa | ∵ Opposite angles of a cyclic quadrilateral are supplementary

$$\therefore \angle ADC = \angle ABC = 90^{\circ}$$

**Given:** ABC is a triangle and P is a point on the side BC such that AB = AP. AP produced meets the circumcircle of  $\triangle ABC$  at Q.

To Prove: CP=CQ



**Proof:** In  $\triangle ABP$  and  $\triangle CQP$ ,

$$\angle BAP = \angle QCP$$

Angles in the same segment of a circle are equal

$$\angle ABP = \angle CPQ$$

$$\therefore \qquad \Delta ABP \cong \Delta CPQ$$

$$\frac{AB}{CO} = \frac{BP}{OP} = \frac{AP}{CP}$$

 $\frac{D}{CQ} = \frac{BP}{QP} = \frac{AP}{CP}$   $| \because \text{ Corresponding sides of two similar triangles are proportional}$   $\frac{AB}{CQ} = \frac{AP}{CP}$   $AB = AP \qquad | \text{ Given}$  CQ = CP

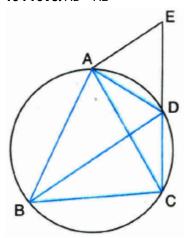
$$\Rightarrow \frac{AB}{CO} = \frac{AP}{CP}$$

But

:.

**Given:** D is a point on the circumference of circumcircle of  $\triangle ABC$  in which AB = AC such that B and D are on opposite sides of AC. CD is produced to point E such that CE = BD.

To Prove: AD = AE



**Proof:** In  $\triangle ACE$  and  $\triangle ABD$ ,

$$\angle ACE = \angle ABD$$

| Angles in the same segment of a circle are equal

AC=AB

I Given

CE=BD

I Given

 $\therefore \quad \Delta ACE \cong \Delta ABD$ 

| SAS congruence rule

∴ AE=AD

**ICPCT** 

48) **Given:** O is the centre of a circle.

**To Prove:** x + y = z

**Proof:**  $\angle 3 = \angle 4$ 

Angles in the same segment of a circle are equal

$$\angle z = 2 \angle 3$$

$$\Rightarrow$$
  $\angle z = \angle 3 + \angle 3$ 

$$\Rightarrow$$
  $\angle z = \angle 3 + \angle 4$ 

....(1)

Now 
$$\angle y = \angle 3 + \angle 1$$

....(2)

An exterior angle of a triangle is equal to the sum of its two interior opposite angles

(1) - (2) gives

$$\angle z - \angle y = \angle 4 - \angle 1$$

As 
$$4 = \angle x + \angle 1 \Rightarrow \angle 4 - \angle 1 = \angle x$$

An exterior angle of a triangle is equal to the sum of its two interior opposite angles

$$\Rightarrow \angle 4 - \angle 1 = \angle x$$

....(4)

From (3) and (4),

$$\angle z - \angle y = \angle x$$

$$\Rightarrow \quad \angle x + \angle y = \angle z$$