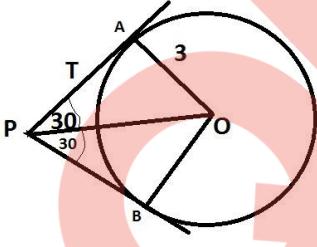
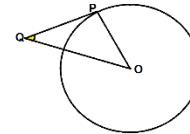


**MARKING SCHEME SQP
MATHEMATICS (STANDARD)**

2020-21

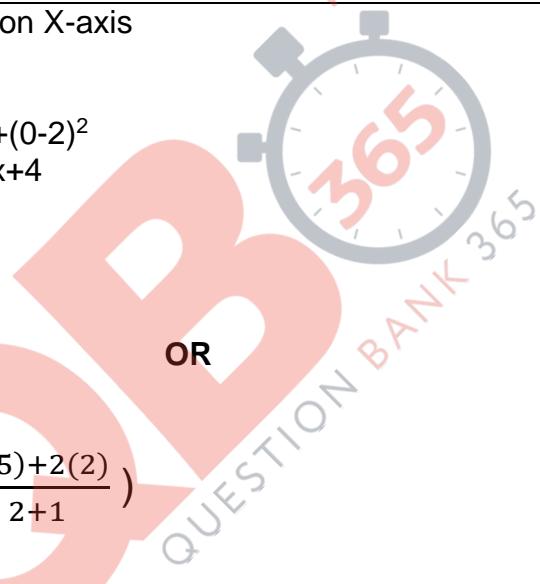
CLASS X

S.NO.	ANSWER	MARKS
Part-A		
1.	(LCM)(3) =180 LCM=60 OR Four decimal places	$\frac{1}{2}$ $\frac{1}{2}$ 1
2.	$\alpha+\beta=k/3$ $3=k/3$ $K=9$	$\frac{1}{2}$ $\frac{1}{2}$
3.	$\begin{array}{r} 3 & 1 & 3 \\ \underline{-} & \underline{-} & \cancel{\underline{-}} \\ 6 & k & 8 \\ \underline{-} & \underline{-} & \\ 6 & k & \\ K=2 & & \end{array}$	$\frac{1}{2}$ $\frac{1}{2}$
4.	Let the cost of 1 chair=Rs.x And the cost of 1 table=Rs. y $3x+y=1500$ $6x+y=2400$	$\frac{1}{2}$ $\frac{1}{2}$
5.	$a_n=a+(n-1)d$ $0=27+(n-1)(-3)$ $30=3n$ $n=10$ 10^{th} OR $a_n=a+(n-1)d$ $4=a+6(-4)$ $a=-28$	$\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$
6.	$9x^2+6kx+4=0$ $(6k)^2-4\times 9\times 4=0$ $36k^2=144$ $K^2=4$ $K=\pm 2$	$\frac{1}{2}$ $\frac{1}{2}$

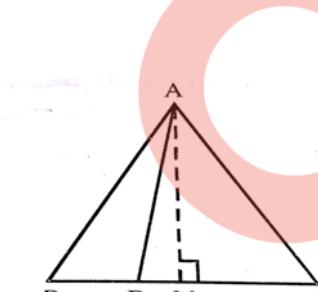
<p>7.</p> $x^2 + 7x + 10 = 0$ $x^2 + 5x + 2x + 10 = 0$ $(x+5)(x+2) = 0$ $X = -5, x = -2$	<p>OR</p> $3ax^2 - 6x + 1 = 0$ $(-6)^2 - 4(3a)(1) < 0$ $12a > 36 \Rightarrow a > 3$	$\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$
<p>8.</p> $PQ = PT$ $PL + LQ = PM + MT$ $PL + LN = PM + MN$ $\text{Perimeter}(\triangle PLM)$ $= PL + LM + PM$ $= PL + LN + MN + PM$ $= 2(PL + LN)$ $= 2(PL + LQ)$ $= 2 \times 28 = 56 \text{ cm}$		$\frac{1}{2}$ $\frac{1}{2}$
<p>9.</p>  <p>In $\triangle PAO$ $\tan 30^\circ = AO/PA$ $1/\sqrt{3} = 3/PA$ $PA = 3\sqrt{3} \text{ cm}$</p>	<p>OR</p>  <p>In $\triangle OPQ$ $\angle P + \angle Q + \angle O = 180^\circ$ $2\angle Q + \angle P = 180^\circ$ $2\angle Q + 90^\circ = 180^\circ$ $2\angle Q = 90^\circ$ $\angle Q = 45^\circ$</p>	$\frac{1}{2}$ $\frac{1}{2}$

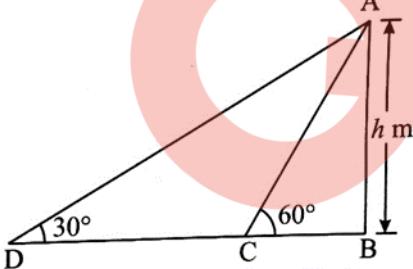
10.	$\frac{AD}{BD} = \frac{AE}{CE}$ $\frac{3}{4.5} = \frac{2}{CE}$ $CE = 3\text{cm}$	$\frac{1}{2}$ $\frac{1}{2}$
11.	8:5	1
12.	$\sin 30^\circ + \cos B = 1$ $\frac{1}{2} + \cos B = 1$ $\cos B = 1/2$ $B = 60^\circ$	$\frac{1}{2}$ $\frac{1}{2}$
13.	$x+y$ $= 2\sin^2\theta + 2\cos^2\theta + 1$ $= 2(\sin^2\theta + \cos^2\theta) + 1$ $= 3$	$\frac{1}{2}$ $\frac{1}{2}$
14.	length of arc $= \theta/360^\circ(2\pi r)$ $= 60/360(2\pi \times 22/7 \times 21)$ $= 22\text{ cm}$	$\frac{1}{2}$ $\frac{1}{2}$
15.	$\pi R^2 H = 12 \times 4 / 3 \pi r^3$ $1 \times 1 \times 16 = 4/3 \times r^3 \times 12$ $r^3 = 1$ $r = 1$ $d = 2\text{cm}$	$\frac{1}{2}$ $\frac{1}{2}$
16.	probability of getting a doublet $= 1/6$ OR probability of getting a black queen $= 2/52 = 1/26$	1
17.	(a) iii) $(15/2, 33/2)$ (b) i) 4 (c) iii) 16 (d) iv) $(2.0, 8.5)$ (e) ii) $x-13=0$	1x4=4
18.	(a) iii) 15 cm (b) iv) They are not the mirror image of one another (c) ii) Their altitudes have a ratio a:b (d) iv) 5m (e) iii) 6m	
19.	(a) ii) $(4, -2)$ (b) i) Intersects x-axis (c) iii) parabola	

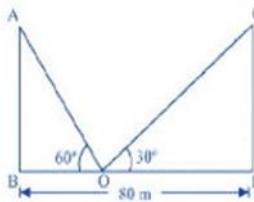
	(d) ii) $x^2 - 36$	
	(e) iii) 0	
20.	(a) iii) 43	1x4=4
	(b) iii) 60	
	(c) ii) Median	
	(d) iii) 80	
	(e) iii) 31	

	Part-B	
21.	$4=2 \times 2$ $7=7 \times 1$ $14=2 \times 7$ $LCM=2 \times 2 \times 7=28$ The three bells will ring together again at 6:28 am	$\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$
22.	Let P(x,0) be a point on X-axis $PA=PB$ $PA^2=PB^2$ $(x-2)^2+(0+2)^2=(x+4)^2+(0-2)^2$ $X^2+4-4x+4=x^2+16+8x+4$ $-4x+4=8x+16$ $X=-1$ $P(-1,0)$	$\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$
	 OR	
	$PR:QR=2:1$ $R\left(\frac{1(-2)+2(3)}{2+1}, \frac{1(5)+2(2)}{2+1}\right)$ $R(4/3, 3)$	$\frac{1}{2}$ 1 $\frac{1}{2}$
23.	Sum of zeroes = $5-3\sqrt{2}+5+3\sqrt{2}=10$ Product of zeroes = $(5-3\sqrt{2})(5+3\sqrt{2})= 7$ $P(x)=X^2-10x+7$	$\frac{1}{2}$ 1 $\frac{1}{2}$
24.		Line seg=1/2 Circles=1/2 Tangents =1/2+ $\frac{1}{2}$

<p>25.</p> <p> $\tan A = 3/4 = 3k/4k$ $\sin A = 3k/5k = 3/5, \cos A = 4k/5k = 4/5$ $1/\sin A + 1/\cos A$ $= 5/3 + 5/4$ $= (20+15)/12$ $= 35/12$ </p> <p style="text-align: center;">OR</p> <p> $\sqrt{3} \sin \theta = \cos \theta$ $\sin \theta / \cos \theta = 1/\sqrt{3}$ $\tan \theta = 1/\sqrt{3}$ $\theta = 30^\circ$ </p>	$\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$
<p>26.</p> <p> $\angle A = \angle OPA = \angle OSA = 90^\circ$ Hence, $\angle SOP = 90^\circ$ Also, AP=AS Hence, OSAP is a square AP=AS=10cm CR=CQ=27cm BQ=BC-CQ=38-27=11cm BP=BQ=11 cm X=AB=AP+BP=10+11=21 cm </p>	$\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$
<p>27.</p> <p> Let $2-\sqrt{3}$ be a rational number We can find co-prime a and b ($b \neq 0$) such that $2-\sqrt{3} = a/b$ $2-a/b = \sqrt{3}$ So we get, $(2a-b)/b = \sqrt{3}$ Since a and b are integers, we get $(2a-b)/b$ is irrational and so $\sqrt{3}$ is rational. But $\sqrt{3}$ is an irrational number Which contradicts our statement Therefore $2-\sqrt{3}$ is irrational </p>	$\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$
<p>28.</p> <p> $3x^2 + px + 4 = 0$ $3(2/3)2 + p(2/3) + 4 = 0$ $4/3 + 2p/3 + 4 = 0$ $P = -8$ $3x^2 - 8x + 4 = 0$ $3x^2 - 6x - 2x + 4 = 0$ $X = 2/3$ or $x = 2$ Hence, $x = 2$ </p>	$\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$

	OR	
	$\alpha + \beta = 5 \quad \dots(1)$ $\alpha - \beta = 1 \quad \dots(2)$ Solving (1) and (2), we get $\alpha = 3$ and $\beta = 2$ also $\alpha\beta = 6$ or $3(k-1) = 6$ $k-1=2$ $k=3$	$\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$
29.	<p>Area of 1 segment = area of sector – area of triangle $= (90^\circ/360^\circ)\pi r^2 - \frac{1}{2} \times 7 \times 7$ $= 1/4 \times 22/7 \times 7^2 - \frac{1}{2} \times 7 \times 7$ $= 14 \text{ cm}^2$</p> <p>Area of 8 segments = $8 \times 14 = 112 \text{ cm}^2$</p> <p>Area of the shaded region = $14 \times 14 - 112$ $= 196 - 112 = 84 \text{ cm}^2$</p> <p>(each petal is divided into 2 segments)</p>	$\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$
30.	<p>$\Delta ABC \sim \Delta DEF$</p> $\frac{\text{Perimeter } (\Delta ABC)}{\text{Perimeter } (\Delta DEF)} = \frac{AB+BC+CA}{DE+EF+FD} = \frac{AB}{DE}$ $\frac{25}{15} = \frac{9}{X}$ $X = 5.4 \text{ cm}$ $DE = 5.4 \text{ cm}$ <p style="text-align: center;">OR</p>  <p>Construction-Draw $AM \perp BC$ $BD \perp 1/3 BC$, $BM = 1/2 BC$ In ΔABM,</p> $AB^2 = AM^2 + BM^2$ $= AM^2 + (BD + DM)^2$ $= AM^2 + DM^2 + BD^2 + 2BD \cdot DM$ $= AD^2 + BD^2 + 2BD(BM - BD)$ $= AD^2 + (BC/3)^2 + 2 \cdot BC/3 \cdot (BC/2 - BC/3)$ $= AD^2 + 2BC^2/9$ $= AD^2 + 2AB^2/9$ <p>Hence, $7AB^2 = 9AD^2$</p>	$\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$

31. <table border="1" style="width: 100%; border-collapse: collapse;"> <thead> <tr> <th style="text-align: left;">Class</th><th style="text-align: center;">Frequency</th><th style="text-align: center;">Cumulative frequency</th><th style="text-align: right; vertical-align: bottom;">1</th></tr> </thead> <tbody> <tr> <td>0-5</td><td style="text-align: center;">12</td><td style="text-align: center;">12</td><td style="text-align: right; vertical-align: bottom;">1</td></tr> <tr> <td>5-10</td><td style="text-align: center;">a</td><td style="text-align: center;">12+a</td><td style="text-align: right; vertical-align: bottom;">1</td></tr> <tr> <td>10-15</td><td style="text-align: center;">12</td><td style="text-align: center;">24+a</td><td style="text-align: right; vertical-align: bottom;">1</td></tr> <tr> <td>15-20</td><td style="text-align: center;">15</td><td style="text-align: center;">39+a</td><td style="text-align: right; vertical-align: bottom;">1</td></tr> <tr> <td>20-25</td><td style="text-align: center;">b</td><td style="text-align: center;">39+a+b</td><td style="text-align: right; vertical-align: bottom;">1</td></tr> <tr> <td>25-30</td><td style="text-align: center;">6</td><td style="text-align: center;">45+a+b</td><td style="text-align: right; vertical-align: bottom;">1</td></tr> <tr> <td>30-35</td><td style="text-align: center;">6</td><td style="text-align: center;">51+a+b</td><td style="text-align: right; vertical-align: bottom;">1</td></tr> <tr> <td>35-40</td><td style="text-align: center;">4</td><td style="text-align: center;">55+a+b</td><td style="text-align: right; vertical-align: bottom;">1</td></tr> <tr> <td>Total</td><td style="text-align: center;">70</td><td></td><td></td></tr> </tbody> </table>	Class	Frequency	Cumulative frequency	1	0-5	12	12	1	5-10	a	12+a	1	10-15	12	24+a	1	15-20	15	39+a	1	20-25	b	39+a+b	1	25-30	6	45+a+b	1	30-35	6	51+a+b	1	35-40	4	55+a+b	1	Total	70			$55+a+b=70$ $a+b=15$ $\text{median} = l + \frac{\frac{N}{2} - cf}{f} \times h$ $16 = 15 + \frac{35-24-a}{15} \times 5$ $1 = (11-a)/3$ $A=8$ $55+a+b=70$ $55+8+b=70$ $B=7$	½ ½ ½ ½ ½ ½
Class	Frequency	Cumulative frequency	1																																							
0-5	12	12	1																																							
5-10	a	12+a	1																																							
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35-40	4	55+a+b	1																																							
Total	70																																									
32.  Let AB=candle C and D are coins $\tan 60^\circ = AB/BC = h/b$ $\sqrt{3} = h/b$ $H = b\sqrt{3}$ ----- (1) $\tan 30^\circ = AB/BD = h/a$ $1/\sqrt{3} = h/a$ $H = a/\sqrt{3}$ ----- (2) Multiplying (1) and (2), we get $H^2 = b\sqrt{3} \times a/\sqrt{3}$ $H^2 = b a$ $H = \sqrt{ab} \text{ m}$	½ ½ ½ ½ ½ ½																																									

<p>33.</p> $\text{Mode} = l + \frac{f_1 - f_0}{2f_1 - f_2 - f_0} \times h$ $67 = 60 + \frac{15-x}{30-12-x} \times 10$ $7 = \frac{15-x}{18-x} \times 10$ $7x(18-x) = 10(15-x)$ $126 - 7x = 150 - 10x$ $3x = 150 - 126$ $3x = 24$ $x = 8$	$\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$
<p>34.</p>  <p>Let BD=river AB=CD=palm trees=h BO=x OD=80-x In $\triangle ABO$, $\tan 60^\circ = h/x$ $\sqrt{3} = h/x$ ----- (1) $H = \sqrt{3}x$ In $\triangle CDO$, $\tan 30^\circ = h/(80-x)$ $1/\sqrt{3} = h/(80-x)$ ----- (2) Solving (1) and (2), we get $x=20$ $H = \sqrt{3}x = 34.6$ the height of the trees=h=34.6m $BO=x=20m$ $DO=80-x=80-20=60m$</p>	$\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$

	OR	
	<p>Let AB=Building of height 50m RT=tower of height= h m BT=AS=x m AB=ST=50 m RS=TR-TS=(h-50)m In $\triangle ARS$, $\tan 30^\circ = RS/AS$ $1/\sqrt{3} = (h-50)/x$ ----- (1) In $\triangle RBT$, $\tan 60^\circ = RT/BT$ $\sqrt{3} = h/x$ ----- (2)</p> <p>Solving (1) and (2), we get $h = 75$ from (2) $x=h/\sqrt{3}$ $=75/\sqrt{3}$ $=25\sqrt{3}$ Hence, height of the tower=h=75m Distance between the building and the tower=$25\sqrt{3}=43.25m$</p>	1 $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$
35.	<p>For pipe , $r = 1\text{cm}$ Length of water flowing in 1 sec, $h=0.7\text{m}=7\text{cm}$ Cylindrical Tank, $R=40\text{ cm}$, rise in water level=H Volume of water flowing in 1 sec= $\pi r^2 h = \pi \times 1 \times 1 \times 70$ $=70\pi$ Volume of water flowing in 60 sec= $70\pi \times 60$ $\pi r^2 H = \pi \times 40 \times 40 \times H$ Volume of water in Tank= $\pi r^2 H = \pi \times 40 \times 40 \times H$ $\pi \times 40 \times 40 \times H = 70\pi \times 60 \times 30$ $H=78.75\text{cm}$</p>	$\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$

36.	<p>Let speed of the boat in still water =x km/hr, and Speed of the current =y km/hr Downstream speed =($x+y$) km/hr Upstream speed =($x-y$) km/hr $\frac{24}{x+y} + \frac{16}{x-y} = 6$-----(1)</p> <p>$\frac{36}{x+y} + \frac{12}{x-y} = 6$-----(2)</p> <p>Let $\frac{1}{x+y} = u$ and $\frac{1}{x-y} = v$</p> <p>Put in the above equation we get, $24u+16v=6$ Or, $12u+8v=3$... (3) $36u+12v=6$ Or, $6u+2v=1$... (4) Multiplying (4) by 4, we get, $24u+8v=4v$... (5) Subtracting (3) by (5), we get, $12u=1$ $\Rightarrow u=1/12$ Putting the value of u in (4), we get, $v=1/4$ $\Rightarrow \frac{1}{x+y} = \frac{1}{12}$ and $\frac{1}{x-y} = \frac{1}{4}$ $\Rightarrow x+y=12$ and $x-y=4$ Thus, speed of the boat in still water = 8 km/hr, Speed of the current = 4 km/hr</p>	$\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$
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