RD SHARMA
Solutions
Class 7 Maths
Chapter 20
Ex 20.3

Q1: Find the area of a parallelogram with base 8 cm and altitude 4.5 cm.

A1: We have, Base = 8 cm and altitude = 4.5 cm Thus, Area of the parallelogram = Base x Altitude = 8 cm x 4.5 cm = 36 cm²

- Q2: Find the area in square metres of the parallelogram whose base and altitudes are as under
- (i) Base = 15 dm, altitude = 6.4 dm
- (ii) Base = 1 m 40 cm, altitude = 60 cm

A2:

We have,

(i) Base =
$$15 \text{ dm} = (15 \text{ x } 10) \text{ cm} = 150 \text{ cm} = 1.5 \text{ m}$$

Altitude =
$$6.4 \text{ dm} = (6.4 \text{ x } 10) \text{ cm} = 64 \text{ cm} = 0.64 \text{ m}$$

Thus, Area of the parallelogram = Base x Altitude

$$= 1.5 \text{ m} \times 0.64 \text{ m}$$

 $= 0.96 \text{ m}^2$

(ii) Base =
$$1 \text{ m} 40 \text{ cm} = 1.4 \text{ m} [\text{Since } 100 \text{ cm} = 1 \text{ m}]$$

Altitude =
$$60 \text{ cm} = 0.6 \text{ m}$$

Thus, Area of the parallelogram = Base x Altitude

$$= 1.4 \text{ m x } 0.6 \text{ m}$$

$$= 0.84 \text{ m}^2$$

[Since 100 cm = 1 m]

Q3: Find the altitude of a parallelogram whose area is 54 d m² and base is 12 dm.

A3:

We have,

Area of the given parallelogram = 54 d m^2

Base of the given parallelogram = 12 dm

Altitude of the given parallelogram = Area/Base = 54/12 dm = 4.5 dm

Q4: The area of a rhombus is 28 m². If its perimeter be 28 m, find its altitude.

A4:

We have,

Perimeter of a rhombus = 28 m 4(Side) = 28 m [Since perimeter = 4(Side)]

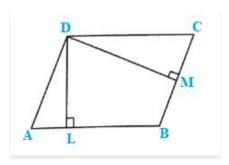
Side = 28 m4 = 7 m

Now, Area of the rhombus = 28 m^2

(Side x Altitude) = 28 m^2 (7 m x Altitude) = 28 m^2

Altitude = 28 m 27 m = 4 m

Q5: In Fig., ABCD is a parallelogram, DL \perp AB and DM \perp BC. If AB = 18 cm, BC = 12 cm and DM = 9.3 cm, find DL.



A5: We have,

Taking BC as the base, BC = 12 cm and altitude DM = 9.3 cm

Area of parallelogram ABCD = Base x Altitude = $(12 \text{ cm x } 9.3 \text{ cm}) = 111.6 \text{ c m}^2$ — (i)

Now, Taking AB as the base,

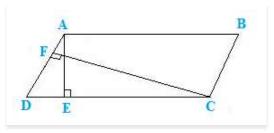
We have, Area of the parallelogram ABCD = Base x Altitude

$$= (18 \text{ cm x DL})$$
 —(ii)

From (i) and (ii), we have $18 \text{ cm x DL} = 111.6 \text{ c m}^2$

DL = 111.6 cm 218 cm =6.2 cm

Q6: The longer side of a parallelogram is 54 cm and the corresponding altitude is 16 cm. If the altitude corresponding to the shorter side is 24 cm, find the length of the shorter side.



A6: We have,

ABCD is a parallelogram with the longer side AB = 54 cm and corresponding altitude AE = 16 cm. The shorter side is BC and the corresponding altitude is CF = 24 cm.

Area of a parallelogram = base x height.

We have two altitudes and two corresponding bases.

So,

$$\frac{1}{2} \times BC \times CF = \frac{1}{2} \times AB \times AE$$

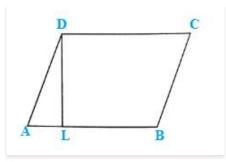
$$\Rightarrow$$
 BC x CF = AB x AE

$$\Rightarrow$$
 BC x 24 = 54 x 16

$$=> BC = (54 \times 16)/24 = 36 \text{ cm}$$

Hence, the length of the shorter side BC = AD = 36 cm.

Q7: In Fig. 21, ABCD is a parallelogram, DL \perp AB. If AB = 20 cm, AD = 13 cm and area of the parallelogram is 100 c m², find AL.



A7: We have,

ABCD is a parallelogram with base AB = 20 cm and corresponding altitude DL.

It is given that the area of the parallelogram ABCD = $100 \text{ c} \text{ m}^2$

Now, Area of a parallelogram = Base x Height

$$100 \text{ c m}^2 = AB \text{ x DL}$$

 $100 \text{ c m}^2 = 20 \text{ cm x DL}$

$$DL = 100 \text{ c m}^2 = 5 \text{ cm}$$

Again by Pythagoras theorem, we have,

$$(AD)^2 = (AL)^2 + (DL)^2$$

$$=>$$
 $(13)^2 = (AL)^2 + (5)^2$

$$(AL)2=(13)^2-(5)^2$$

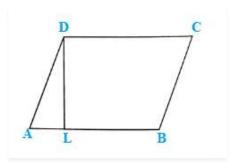
$$= 169 - 25 = 144$$

$$(AL)^2 = (12)^2$$

$$AL = 12 \text{ cm}$$

Hence, length of AL is 12 cm.

Q8: In Fig. 21, if AB = 35 cm, AD = 20 cm and area of the parallelogram is 560 cm^2 , find LB.



A8:

We have,

ABCD is a parallelogram with base AB = 35 cm and corresponding altitude DL.

The adjacent side of the parallelogram AD = 20 cm.

It is given that the area of the parallelogram ABCD = $560 \text{ c} \text{ m}^2$

Now, Area of the parallelogram = Base x Height

$$560 \text{ c m}^2 = \text{AB x DL } 560 \text{ c m}^2 = 35 \text{ cm x DL}$$

$$DL = 560 \text{ cm}/235 \text{ cm} = 16 \text{ cm}$$

Again by Pythagoras theorem, we have, $(AD)^2 = (AL)^2 + (DL)^2$

$$(20)^2 = (AL)^2 + (16)^2$$

$$(AL)^2 = (20)^2 - (16)^2$$

$$=400-256$$

= 144

$$(AL)^2 = (12)2$$

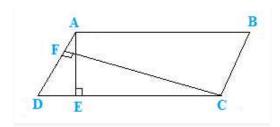
From the figure, AB = AL + LB 35 cm

$$= 12 \text{ cm} + \text{LB}$$

$$LB = 35 \text{ cm} - 12 \text{ cm} = 23 \text{ cm}$$

Hence, length of LB is 23 cm.

Q9: The adjacent sides of a parallelogram are 10 m and 8 m. If the distance between the longer sides is 4 m, find the distance between the shorter sides.



A9: We have,

ABCD is a parallelogram with side AB = 10 m and corresponding altitude AE = 4 m.

The adjacent side AD = 8 m and the corresponding altitude is CF.

Area of a parallelogram = Base x Height

We have two altitudes and two corresponding bases.

So,
$$AD \times CF = AB \times AE = 8 \text{ m } \times CF = 10 \text{ m } \times 4 \text{ m}$$

$$= CF = (10 \times 4)8 = 5 \text{ m}$$

Hence, the distance between the shorter sides is 5 m.

Q10: The base of a parallelogram is twice its height. If the area of the parallelogram is 512 cm², find the base and height.

A10:

Let the height of the parallelogram be x cm.

Then the base of the parallelogram is $2x\ cm$.

It is given that the area of the parallelogram = 512 cm^2

So, Area of a parallelogram = Base x Height

$$512 \text{ c m}^2 = (2x)(x)$$

$$512 \text{ c m}^2 = 2x^2$$

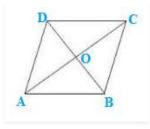
$$X^2 = 512 \text{ cm}^2/2 = 256 \text{ c m}^2$$

$$X^2 = (16 \text{ cm})^2$$

$$X = 16 \text{ cm}$$

Hence, base = $2x = 2 \times 16 = 32$ cm and height = x = 16 cm.

Q11: Find the area of a rhombus having each side equal to 15 cm and one of whose diagonals is 24 cm.



A11:

Let ABCD be the rhombus where diagonals intersect at 0.

Then AB = 15 cm and AC = 24 cm.

The diagonals of a rhombus bisect each other at right angles.

Therefore, triangle A0B is a right-angled triangle, right angled at O such that

$$OA = \frac{1}{2}(AC) = 12 \text{ cm} \text{ and } AB = 15 \text{ cm}.$$

By Pythagoras theorem, we have,

$$(AB)^2 = (OA)^2 + (OB)^2$$

$$(15)^2 = (12)^2 + (OB)^2$$

$$(OB)^2 = (15)^2 - (12)^2$$

$$(OB)^2 = 225 - 144 = 81$$

$$(OB)^2 = (9)^2$$

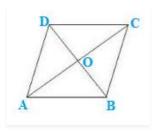
OB = 9 cm

$$BD = 2 \times OB = 2 \times 9 \text{ cm} = 18 \text{ cm}$$

Hence, Area of the rhombus ABCD = $(\frac{1}{2} \times AC \times BD)$

 $= 216 \text{ cm}^2$

Q12: Find the area of a rhombus, each side of which measures 20 cm and one of whose diagonals is 24 cm.



A12:

Let ABCD be the rhombus whose diagonals intersect at 0.

Then AB = 20 cm and AC = 24 cm.

The diagonals of a rhombus bisect each other at right angles.

Therefore Triangle AOB is a right-angled triangle, right angled at O

Such that;

$$OA = \frac{1}{2} AC = 12 \text{ cm}$$
 and $AB = 20 \text{ cm}$

By Pythagoras theorem, we have,

$$(AB)^2 = (OA)^2 + (OB)^2$$

$$(20)^2 = (12)^2 + (OB)^2$$

$$(OB)^2 = (20)^2 - (12)^2$$

$$(OB)^2 = 400 - 144$$

= 256

$$(OB)^2 = (16)^2$$

$$=> OB = 16 \text{ cm}$$

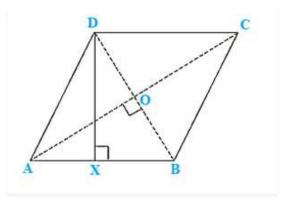
$$BD = 2 \times OB = 2 \times 16 \text{ cm} = 32 \text{ cm}$$

Hence, Area of the rhombus $ABCD = \frac{1}{2} \times AC \times BD$

 $= \frac{1}{2} \times 24 \times 32$

 $= 384 \text{ c m}^2$

Q13: The length of a side of a square field is 4 m. What will be the altitude of the rhombus, if the area of the rhombus is equal to the square field and one of its diagonals is 2 m?



A13: We have,

Area of the rhombus = Area of the square of side 4 m

$$=> \frac{1}{2} \times AC \times 130 = 4 \text{ m}^2$$

$$=> \frac{1}{2} \times AC \times 2 \text{ m} = 16 \text{ m}^2$$

We know that the diagonals of a rhombus are perpendicular bisectors of each other.

$$=> AO = \frac{1}{2} (AC) = 8 \text{ m} \text{ and } BO = \frac{1}{2} (BD) = 1 \text{ m}$$

By Pythagoras theorem, we have:

$$AO^2 + BO^2 = AB^2$$

$$AB^2 = (8 \text{ m})^2 + (1 \text{ m})^2 = 64 \text{ m}^2 + 1 \text{ m}^2 = 65 \text{ m}^2$$

Side of a rhombus =
$$AB = \sqrt{65}$$
 m.

Let DX be the altitude.

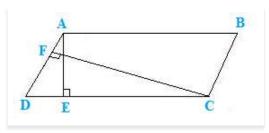
Area of the rhombus = AB x DX 16 m^2

$$=\sqrt{65}$$
m x DX

$$DX = 16/(\sqrt{65}) \text{ m}$$

Hence, the altitude of the rhombus will be $16/\sqrt{65}$ m.

Q14: Two sides of a parallelogram are 20 cm and 25 cm. If the altitude corresponding to the sides of length 25 cm is 10 cm, find the altitude corresponding to the other pair of sides.



A14:

We have,

ABCD is a parallelogram with longer side AB = 25 cm and altitude AE = 10 cm.

As ABCD is a parallelogram. Hence AB = CD (opposite sides of parallelogram are equal).

The shorter side is AD = 20 cm and the corresponding altitude is CF.

Area of a parallelogram = Base x Height

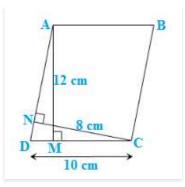
We have two altitudes and two corresponding bases.

So, =
$$AD \times CF = CD \times AE$$

$$CF = 12.5 \text{ cm}$$

Hence, the altitude corresponding to the other pair of the side AD is $12.5\ cm$.

Q15: The base and corresponding altitude of a parallelogram are 10 cm and 12 cm respectively. If the other altitude is 8 cm, find the length of the other pair of parallel sides.



A15: We have,

ABCD is a parallelogram with side AB = CD = 10 cm (Opposite sides of parallelogram are equal) and corresponding altitude AM = 12 cm. The other side is AD and the corresponding altitude is CN = 8 cm.

Area of a parallelogram = Base x Height

We have two altitudes and two corresponding bases.

So.

$$\Rightarrow$$
 AD x CN = CD x AM

$$\Rightarrow$$
 AD x 8 = 10 x 12

$$=> AD = (10 \times 12)/8 = 15 \text{ cm}$$

Hence, the length of the other pair of the parallel side = 15 cm.

Q16: A floral design on the floor of a building consists of 280 tiles. Each tile is in the shape of a parallelogram of altitude 3 cm and base 5 cm. Find the cost of polishing the design at the rate of 50 paise per $\rm cm^2$.

A16:

We have,

Attitude of a tile = 3 cm

Base of a tile = 5 cm

Area of one tile = Attitude x Base = $5 \text{ cm x } 3 \text{ cm} = 15 \text{ c m}^2$

Area of 280 tiles = $280 \times 15 \text{ c m}^2 = 4200 \text{ c m}^2$

Rate of polishing the tiles at 50 paise per c $m^2 = Rs$. 0.5 per c m^2

Thus, Total cost of polishing the design = Rs. (4200×0.5) = Rs. 2100