

Model Question paper

Trigonometry 3

11th Standard

Maths

Reg.No. :

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I. Answer all the questions.

II. Use blue pen only.

Time : 02:30:00 Hrs

Total Marks : 75

10 x 1 = 10

Part - A

- 1) One radian is equal to (in terms of degree).....
(a) $\frac{180^\circ}{11}$ (b) $\frac{\pi}{180^\circ}$ (c) $\frac{180^\circ}{\pi}$ (d) $\frac{11}{180^\circ}$
- 2) $\frac{1}{360}$ of a complete rotation clockwise is.....
(a) -1° (b) -360° (c) -90° (d) 1°
- 3) Area of triangle ABC is.....
(a) $\frac{1}{2}abc \cos C$ (b) $\frac{1}{2}abs \sin C$ (c) $\frac{1}{2}abs \sin C$ (d) $\frac{1}{2}bc \sin B$
- 4) In any triangle ABC, is.....
(a) abc (b) $\frac{abc}{4R}$ (c) $\frac{abc}{2R}$ (d) $\frac{abc}{R}$
- 5) $\cos B$ is equal to.....
(a) $\frac{c^2 + a^2 - b^2}{2ca}$ (b) $\frac{c^2 + b^2 - a^2}{2bc}$ (c) $\frac{a^2 + b^2 - c^2}{2ab}$ (d) $\frac{a^2 + b^2 + c^2}{2ab}$
- 6) Which one of the following is true,
(a) $\cos(A+B) = \cos A + \cos B$ (b) $\cos(A-B) = \cos A - \cos B$ (c) $\cos(A-B) = \cos A + \cos B$ (d) $\cos(A+B) \neq \cos A + \cos B$
- 7) The value of $\sin(-780^\circ)$ is
(a) $\frac{\sqrt{3}}{2}$ (b) $\frac{2}{\sqrt{3}}$ (c) $-\frac{2}{\sqrt{3}}$ (d) $-\frac{\sqrt{3}}{2}$
- 8) $\sin^4 \theta + \cos^4 \theta =$
(a) $\sin^2 \theta \cos^2 \theta$ (b) $1 + 2\sin^2 \theta \cos^2 \theta$ (c) $1 - 2\sin^2 \theta \cos^2 \theta$ (d) $2\cos^2 \theta \sin^2 \theta$
- 9) $\sin 75^\circ - \sin 15^\circ =$
(a) $\sin 60^\circ$ (b) $\cos 105^\circ + \cos 15^\circ$ (c) $\sin 105^\circ - \sin 15^\circ$ (d) $\cos 105^\circ - \cos 15^\circ$
- 10) The value of $\sec \frac{\pi}{4}$ is
(a) $\sqrt{2}$ (b) $\frac{1}{\sqrt{2}}$ (c) $-\sqrt{2}$ (d) $-\frac{1}{\sqrt{2}}$

Part - B

10 x 2 = 20

- 11) Convert the following degree measure into radian measure.
 30°
- 12) Prove that $\sin(45^\circ + A) - \cos(45^\circ + A) = \sqrt{2} \sin A$
- 13) Find $\cos 45^\circ - \cos 30^\circ$ and compare with $\cos 15^\circ$
- 14) If $\sin A = \frac{1}{3}$, $\sin B = \frac{1}{4}$ find $\sin(A+B)$, where A and B are acute.
- 15) Find the general solution of the following equation:
 $\sin 2\theta = \frac{1}{2}$
- 16) Solve the following
 $\cos^2 x + \sin^2 x + \cos x = 0$
- 17) If $a \sin^2 \theta + b \cos^2 \theta = c$ show that $\tan^2 \theta = \frac{c-b}{a-c}$
- 18) Show that $4(\cos^3 20^\circ + \cos^3 40^\circ) = 3(\cos 20^\circ + \cos 40^\circ)$
- 19) Prove that $\sum (b^2 - c^2) \sin^2 A = 0$
- 20) Show that $\tan 75^\circ + \cot 75^\circ = 4$

Part - C

10 x 3 = 30

- 21) Express the following as functions of positive acute angles
 $\cos(1220^\circ)$
- 22) Express the following as functions of positive acute angles
 $\cos(-1050^\circ)$
- 23) Express the following as functions of A:
 $\sec(A - \frac{3\pi}{2})$
- 24) Prove that $\frac{\sin(180^\circ + A) \cdot \cos(90^\circ - A) \cdot \tan(270^\circ - A)}{\sec(540^\circ - A) \cos(360^\circ + A) \operatorname{cosec}(270^\circ + A)} = -\sin A \cos^2 A$

25) Find the value of the following expressions:

$$\cos \frac{\pi}{6} \cdot \cos \frac{\pi}{3} - \sin \frac{\pi}{6} \cdot \sin \frac{\pi}{3}$$

26) Prove the following

$$2\sin 15^\circ \cos 15^\circ = \frac{1}{2}$$

27)

$$\text{Prove that } \cos^2\left(\frac{\pi}{4} - \theta\right) - \sin^2\left(\frac{\pi}{4} - \theta\right) = \sin 2\theta$$

28) If $\tan \alpha = \frac{1}{3}$ and $\tan \beta = \frac{1}{7}$ show that $2\alpha + \beta = \frac{\pi}{4}$

29) Prove that $\tan(A+B) = \frac{\tan A + \tan B}{1 - \tan A \cdot \tan B}$

30) If $\sin \theta = \frac{3}{8}$ and θ is acute, find $\sin 2\theta$?

Part - D

3 x 5 = 15

31) Prove the following: $\frac{1}{1+\sin\theta} + \frac{1}{1-\sin\theta} = 2\sec^2\theta$

32) Prove that $\sin 20^\circ \sin 40^\circ \sin 60^\circ \sin 80^\circ = \frac{3}{16}$

33) In any triangle ABC prove that $\frac{a^2 \sin(B-C)}{\sin A} + \frac{b^2 \sin(C-A)}{\sin B} + \frac{c^2 \sin(A-B)}{\sin C}$

