

Model Question paper

Integral Calculus 3

11th Standard

Maths

Reg.No. :

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I. Answer all the questions.

II. Use blue pen only.

Time : 02:00:00 Hrs

Total Marks : 60

10 x 1 = 10

Part - A

- 1) $\int \frac{1}{e^x} dx = \dots\dots\dots$
 (a) $\log e^x + c$ (b) $-\frac{1}{e^x} + c$ (c) $\frac{1}{e^x} + c$ (d) $x + c$
- 2) $\int \sin 7x \cos 5x \, dx =$
 (a) $\frac{1}{35} \cos 7x \sin 5x + c$ (b) $-\frac{1}{2} \left[\frac{\cos 12x}{12} + \frac{\cos 2x}{2} \right] + c$ (c) $-\frac{1}{2} \left(\frac{\cos 6x}{6} + \cos x \right) + c$ (d) $\frac{1}{2} \left[\frac{\cos 12x}{12} + \frac{\cos 2x}{2} \right] + c$
- 3) $\int \frac{x}{x+x^2} dx = \dots\dots\dots$
 (a) $\tan^{-1}x + c$ (b) $\frac{1}{2} \log(1+x^2) + c$ (c) $\log(1+x^2) + c$ (d) $\log x$
- 4) $\int \tan x \, dx = \dots\dots\dots$
 (a) $\log \cos x + c$ (b) $\log \sec x + c$ (c) $\sec^2 x + c$ (d) $\frac{\tan^2 x}{2} + c$
- 5) $\int \left(\frac{x-1}{x+1} \right) dx = \dots\dots\dots$
 (a) $\frac{1}{2} \left(\frac{x-1}{x+1} \right)^2 + c$ (b) $x - 2\log(x+1) + c$ (c) $\frac{(x-1)^2}{2} \log(x+1) + c$ (d) $x + 2\log(x+1) + c$
- 6) $\int \left(x + \frac{1}{x} \right) dx = \dots\dots\dots + c$
 (a) $\frac{x^2}{2} + \log|x|$ (b) $\frac{x^2}{2}$ (c) $\frac{x^2}{2} + \log x$ (d) $\log x$
- 7) $\int \cos(2x+3) dx = \dots\dots\dots + c$
 (a) $\log|\cos x + \sin x|$ (b) $\log(\cos x + \sin x)$ (c) $\log(\cos x - \sin x)$ (d) $\log|\cos x - \sin x|$
- 8) $\int \frac{4\cos^2 x}{1+\cos x} dx = \dots\dots\dots + c$
 (a) $\log(x + \log \sec x)$ (b) $\log|x + \log \sec x|$ (c) $\log(1 + \cot x)$ (d) $\log|1 + \cot x|$
- 9) $\int (e^{3x} + 1)^2 dx = \dots\dots\dots + c$
 (a) $2(e^{3x} + 1)$ (b) $6(e^{3x} + 1)$ (c) $\frac{e^{6x}}{6} + 2\frac{e^{3x}}{3} + x$ (d) $\frac{1}{(e^{3x} + 1)^3}$
- 10) $\int \frac{\sin^{-1} x}{\sqrt{1-x^2}} dx = \dots\dots\dots + c$
 (a) $(\sin^{-1} x)^2$ (b) $\frac{(\sin^{-1} x)^3}{3}$ (c) $\frac{(\sin^{-1} x)^2}{2}$ (d) $\frac{1}{1-x^2}$

Part - B

5 x 2 = 10

11) Integrate the following with respect to x.

(i) $\left(\frac{1}{x^3} \right)^{\frac{1}{4}}$

12) Integrate the following.

$\sin^2 3x + 4\cos 4x$

13) Integrate the following.

$\frac{1 - \sin x}{1 + \sin x}$

14) Evaluate the following integrals: $\int \frac{\sin 2x}{1 + \sin^2 x} dx$

15) Integrate the followings

$\frac{1}{\sqrt{x^2 + 3x + 10}}$

Part - C

5 x 3 = 15

16) Integrate the following with respect to x.

$\frac{1}{3x+2}$

17) Integrate the following.

$\tan x$

18) Integrate the following

$$\frac{\sin 2x}{a \cos^2 x + b \sin^2 x}$$

19) Integrate the following with respect to x.

$$\operatorname{cosec}(4x+2) \cot(4x+2)$$

20) Integrate the following with respect to x

$$\frac{1}{\tan(2x+3) \sin(2x+3)}$$

Part - D

5 x 5 = 25

21) Integrate the followings with respect to x

$$\tan^{-1} \left(\frac{3x-x^3}{1-3x^2} \right)$$

22) Integrate the following with respect to x.

$$x^6$$

23) Integrate the following:

$$\frac{1}{\sqrt{x^2-9}}$$

24) Integrate $\frac{e^{x/2} - e^{-x/2}}{e^x - e^{-x}}$

25) Integrate $\frac{1}{\sqrt{a^2-x^2}}$

